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#### NEW RULE FOR CUBE ROOT.

#### BY J. B. MOTT, WORTHINGTON, MINNESOTA.

In the following example the ordinary method is pursued till the second figure of the root is found. We then find the triple product (t. p.) by placing the second figure of the root to the right of three times the preceding part of the root and multiplying this by said second figure, and so on for all the triple products, finding one from the other. Thus:

1st trial divisor + 1st t. p. = 1st complete divisor.

1st complete divisor+1st t. p.  $+b^2+2$ nd t. p. = 2nd complete divisor.

2nd complete divisor + 2nd t. p. +  $c^2$  + 3rd t.p. = 3rd com. divisor, &c., placing each t. p. two figures to the right under the preceding divisor; b, c &c., being 2nd, 3rd &c. figures of the root.

Each complete divisor is used as a trial divisor for the next figure of the root. The constant left hand figures of any divisor, used as in simple division, will determine as many more figures of the root.

EXAMPLE.—To find the cube root of 2 to fourteen places of decimals.

```
First trial divisor
                                2(1.259921
    t. p. = 32 \times 2 = 64
                                1000
     com. divisor
1st t. p. +4+2d t. p.,
                                  728
                     8625
2nd complete divisor,
                      45025
                                 )272000
2nd t. p+25+3d t. p., 218831
                                  225125
3rd complete divisor,
                      4721331
                                  )46875000
3rd t. p.+81+4th t. p., 3731211
                                   42491979
4th complete divisor,
                      475864311
                                    )4383021000
                         34765144
                                     4282778799
4th t. p. +81+5th t. p.,
5th complete divisor.
                      47621196244
                                     )100242201000
5th t. p. +4 + 6th t. p.,
                                       95242392488
                           79375561
6th complete divisor,
                      4762198998961
                                       )4999808512000
                                        4762198998961
6th t. p. + 0 + 7th t. p.,
                             3779762
                      4762202778723
                                         )237609513039
7th complete divisor,
```

Dividing, we have  $2376095 \div 47622028 = .04989487 +$ . This united to the root above gives  $\sqrt[3]{2} = 1.25992104989487 +$ .

Remarks on Professor Johnson's Query by R. J. Adcock.—Mr. Jonson's paradox involves two questions, the value of u, and the value of  $du \div dx = \cos ax$ , when  $a = \infty$ . He says "now if  $a = \infty$ , u = 0 independently of x". This I deny. 0 is used to represent both actual zero and

infinitesimal quantities. It cannot however be so used unless it can be shown that no error will result from such use in the particular case. In this case when  $a = \infty$ , u =actual zero or an infinitesimal, that is  $u = 0 \div a$  or some infinitesimal between  $1 \div a$  and  $-1 \div a$ , these infinitesimals depending for their values upon a and x. And the rate at which these infinitesimals change their values is  $du \div dx = \cos ax$ , for all values of a and x.

When a is infinite, that is greater than any assignable number, then a is indeterminately great, and by consequence indeterminate;  $\cos ax$  is the cosine of an arc in a given circle, the arc being as indeterminate as a, and therefore  $\cos ax$  is indetermiate both in "form" and value, and from the given conditions can no more be affirmed to be zero than any other value between +1 and -1. There being no preference or reason for the termination of the arc ax in one part of the circumference rather than another. Mathematics having to deal with truth, like the "Scripture is of no private interpretation".

### DIFFERENTIATION OF THE LOGARITHM OF A VARIABLE.

BY PROF. LABAN E. WARREN, COLBY UNIV., WATERVILLE, ME.

To differentiate the logarithm of a variable, let  $y = e^x$ ;  $\therefore x = \log_e y; \quad dx = d(\log_e y).$   $y + dy = e^{x+dx}, \quad dy = e^{x+dx} - e^x \text{ or } dy = e^x(e^{dx} - 1),$   $e^{dx} = 1 + dx + \frac{dx^2}{2!} + \frac{dx^3}{3!} + \text{\&c., or } e^{dx} = 1 + dx;$   $dy = e^x(1 + dx - 1), \text{ or } dy = e^x dx = y dx, \text{ or } dx = dy \div y,$ but  $dx = d(\log_e y);$   $\therefore d(\log_e y) = dy \div y, \text{ differential of Napierian logarithm.}$   $\log_{10} y = m(\log_e y); \quad d(\log_{10} y) = m d(\log_e y);$   $\therefore d(\log_{10} y) = m \frac{dy}{y}, \text{ differential of common log.}$ 

## SOLUTIONS OF PROBLEMS NUMBER TWO.

Solutions of problems in No. 2 have been received as follows:

From Prof. L. G. Barbour, 434; Prof. W. P. Casey, 430, 431, 433; G. E. Curtis, 429, 434; Geo. Eastwood, 431; Wm. Hoover, 429, 430; Prof. P. H. Philbrick, 429, 430, 431, 433, 434; Prof. E. B. Seitz, 430, 431, 433, 435; Prof. J. Scheffer, 428, 430, 431, 433.